### SLOW BEAM EXTRACTION FROM TARN II

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### Abstract

A slow beam extraction system for TARN II is under construction to provide heavy-ion beams (p, $\alpha \sim$ Ne) at intermediate energy (150~350 MeV/u). The third order resonance extraction with tuning of lattice quadrupole magnets is to be used. The emittance of the extracted beam and the extraction efficiency are estimated to be  $5\pi \text{ mm} \cdot \text{mrad}$  and more than 89%, respectively.

### Introduction

At Institute for Nuclear Study, University of Tokyo, a synchrotron/cooler ring, TARN II, has been under construction since 1984. TARN II aims at acceleration of heavy ions up to Ne into the intermediate energy region (150~350 MeV/u) and capability to reduce the emittance and momentum spread of the ion beam with an electron beam cooling.<sup>1</sup> In order to respond to the demands for heavy ions with intermediate energy to utilize for fundamental research of biomedical irradiation, a slow beam extraction system has been designed and its hardware equipments have been already under construction.<sup>2,3</sup>

In the present paper, the scheme of the slow beam extraction adopted at TARN II is described at first. Then the results of beam tracking simulation based on this system are presented. Finally, the expected quality of the extracted beam is given.

### Slow Beam Extraction System

The layout of the slow beam extraction system is shown in Fig. 1 together with the arrangement of the main magnets of TARN II. The essential parameters of this extraction system are listed up in Table 1.

The operating point of TARN II at the injection stage is chosen to be around (1.75, 1.80). If the halfinteger resonance ( $\nu_{\rm H}=3/2$ ) is to be used, it needs crossing of the third order resonance ( $\nu_{\rm H}=5/3$ ), which requires additional care for compensating the third order stopband. Mainly from this reason, the third order resonant beam extraction is adopted here.

The extraction process is performed in the following procedure.

- a) Nearly at the end of beam acceleration stage, such an orbit bump as makes aperture minimum at the entrance of an electrostatic septum (ES) is made by exciting bump coils 1, 2 and 3, which are wound
  - at backlegs of main dipole magnets.



Fig. 1 Layout of the Slow Extraction System of TARN II.



- Fig. 2 Behaviour of the injection beam with emmitance of  $150\pi$  mm  $\cdot$  mrad in transverse phase space with full excitation of the resonance exciter.
  - b) The operating point is moved from (1.75, 1.80) to (1.6667, 1.80) by changing the excitation currents of the quadrupole magnets in the lattice after the completion of process a). Precise tune change is made by exciting additional coils attached to the main quadrupole magnets after reaching close enough to the resonance ( $\gamma = 5/3$ ).
  - c) Beams which have deviated to the distance more than 75 mm outside from the central orbit at the entrance of the ES are deflected outward as large as 5.8 mrad by the static high voltage of the ES.
  - d) A septum magnet (SM), which is located almost one cell downstream from the ES to accept all the deflected beams in procedure c), gives much larger deflection angle (85 mrad) to guide the beam outside the ring.

A sextupole magnet for excitation of the third order resonance,  $\gamma$   $_{\rm H}=5/3,$  is located at the position indicated in Fig. 1. Throughout the whole process from injection to extraction, it is energized at the level corresponding to the extraction beam energy. The effect of existence of such a rather strong sextupole field during injection and acceleration stage is investigated by beam tracking with a computer. Typical result is shown in Fig. 2. It is seen that although the effect of nonlinear magnetic field is observed, the beam motion is still bounded and stable acceleration can be expected with existence of such a sextupole In this situation, rather large chromaticities field. in both horizontal and vertical directions are anticipated, however tune spread of the beam with fractional momentum spread of  $\pm 0.2\%$  remains well inside the triangular region surrounded with nearby resonances as shown in Fig. 3. So we have decided to use the sextupole magnet with DC characteristics<sup>4</sup> as a resonance exciter.

## Table 1

Parameters of Slow Extraction System of TARN II

Ion Species Beam Energy Extraction Scheme Operating Point Septum Position Beam Emittance

Momentum Spread

p,  $\alpha \sim \text{Ne}$ 150 ~ 350 MeV/u Third Order Resonance Extraction (1.6667, 1.80) 75 mm outside from centeral orbit Circulating Beam  $\leq 50\pi$  mm · mrad Extracted Beam ~  $5\pi$  mm · mrad  $\pm 0.2\%$ 



Hardware equipments for the extraction system described above are listed up in Table 2 with their main specifications.

### Beam Tracking during the Extraction Process

At TARN II, the horizontal aperture is basically designed to be  $\pm 100$  mm, but it is limited at much smaller value as  $\pm$  70 mm at several places where electrostatic pick-ups are installed. It is enevitable to investigate the beam trajectory just before extraction over the whole circumference and make it sure it can safely circulate in the ring until it enters into the aperture of the ES. For this purpose, beam tracking is performed. Beam motion in transverse phase spaces is traced with use of transfer-matrix formalism. The nonlinear element is treated with thin lens approximation. The beam momentum is kept at the certain value because during the extraction process no RF voltage is to be applied to make flat time structure of the extracted beam. The horizontal tune of the ring is gradually shifted from 1.75 to 1.6667 by changing the excitation levels of quadrupole magnets linearly. In Fig. 4, typical example is given for such a beam with central momentum and emittance of  $50\pi\,\mathrm{mm}\cdot\mathrm{mrad}$ . As the result of the procedure (a) in the previous section, the deviation of the bump orbit from the central orbit and its derivative at the entrance of the ES as large as 22 mm and -5.2 mrad are taken into account. The behaviour of the beam in the horizontal transverse phase space at the entrance of the ES is shown in Fig. 4(a) through the whole process from just after acceleration to the end of extraction. In order to clarify this situation, the beam behaviour is displayed separately according to the horizontal tune in Fig. 4 (b) and (c). The beam's motion is almost not affected by the nonlinear field of the resonance exciter and the beam circulates on a ellipse as shown in Fig. 4(b) while  $\nu$   $_{\rm H}$ remains higher than 1.68. Then the motion begins to be distorted and the ellipse is distorted to triangular shape little by little after the distance from the resonance in the tune diagram approaches closer than

## Table 2

# Hardware Equipments for Slow Beam Extraction

Sextupole Magnet	$B''L/B\rho = 0.3015 \ 1/m^2$ (DC mode)
Electrostatic Septum	$E = 70 \sim 85 \text{ kV/cm}, L = 1.0 \text{ m},$
	Deflection Angle = 5.8 mrad,
	Septum Thickness = 0.15 mm
Septum Magnet	B = 5 kG, L = 1.0 m,
•	Deflection Angle = 85.2 mrad,
	Septum Thickness = 9 mm
Bump Coil 1	Deflection Angle = 5.4 mrad
<i>"</i> 2	" =-7.1 mrad
// 3	'' = 7.1  mrad

0.008. Finally after the tune difference comes to 0.0033, the beam begins to move on the separatrix shown in Fig. 4(c) and its amplitude blows up. For the purpose of checking the validity of such tracking, an analytical calculation of the unstable fixed points and the separatrix is performed<sup>5</sup> assuming the beam emittance of  $50\pi$  mm·mrad and the same orbit bump as the tracking. The solid lines in Fig. 4(c) show the ones obtained by such a calculation, which coincide well in global feature with the tracking result.

When the deviation of the beam from the central orbit at the entrance of the ES exceeds the septum position of the ES(75 mm in the present case), the results are traced back to three turns before and the beam positions at the whole circumference in these turns are calculated. In Fig. 5, a typical example of such calculation is shown. From the figure, it is seen that the largest deviation of the beam position at other places than the ES occurs at the position of



(b)  $\nu_{\rm H} = 1.75 \sim 1.68$ 







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Fig. 5 Beam positions in the horizontal direction during last three turns just before extraction and after deflection by extraction septums.

 $Q_F$  magnet just before the ES and its size is assured to remain inside of the vacuum chamber in the  $Q_F$  magnet (±95 mm). The beam positions in such three turns are studied for all the beams with fractional momentum spread of ±0.2% and emittance from  $5\pi$  (simulates beam with very small amplitude) to  $50\pi$  mm·mrad and are checked to be well inside of the aperture of the various equipments distributed around the ring including the electrostatic pick-ups with the minimum aperture.

# Characteristics of the Extracted Beam

The turn separation (the amplitude growth of beam in three turns) just before entering into the aperture of the ES can be studied at the same time with the beam tracking described in the previous section. The results are summarized in Table 3 for various beam conditions. The turn separation of the beam is calculated analytically with the treatment given by D. A. Edwards<sup>6</sup>. The calculated result for the beam with emittance of  $50\pi$  mm·mrad and central momentum is 3 mm, which seems to be in good agreement with the above result. The septum wire of the ES is 0.09 mm in diameter, however its effective thickness is estimated to be 0.15 mm considering the deformation and misalignment of the wire. The extraction efficiency given in Table 3 is calculated assuming this value.

In order to estimate the emittance of the extracted beam, beam location in the horizontal transverse phase space at the exit of the SM is calculated as shown in Fig. 6. In the calculation, the ap





# Table 3

### Turn Separation and Extraction Efficiency

Condition c	of	Turn	Extraction
Circulating	Beam	Separation(mm)	Efficiency(%)
Emittance	$\Delta p/p$		
(mm · mrad)	(%)		
$5\pi$	0.2	2.5	94
$5\pi$	0.0	4.0	96
$5\pi$	-0.2	6.3	98
$50\pi$	0.2	1.4	89
$50\pi$	0.0	2.6	94
$50\pi$	-0.2	4.2	96

plied electric field on the ES is changed from 85 kV/cm to 70 kV/cm from the beginning to the end of the extraction process to compensate the angle difference of the extracted beam at the entrance of ES depending on the oscillation amplitude of the beam before extraction. During the slow extraction, the beam with the largest emittance of  $50\pi$  mm  $\cdot$  mrad begins to be extracted at first and then gradually beams of the smaller eminttance are extracted according to the approach of the horizontal tune to the resonance and finally very small emittance (here we use  $5\pi$  mm  $\cdot$  mrad instead of 0 from computational reason) beam near the equilibrium orbit is extracted. The instantaneous beam emittance is estimated  $\sim 2\pi~{\rm mm\cdot mrad}.$  However, it varies depending on time. Time integrated emittance of the extracted beam is estimated  $\sim 5\pi$  mm  $\cdot$  mrad. In Fig. 7, the beam trajectory of the extracted beam is shown for the straight section where the SM is located. It is seen that all the beams deflected by the ES located upstream are guided into the aperture of the SM clearing its septum thickness of 9 mm.



Fig. 7 Orbits of the extracted beam at the straight section where the SM is located.

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